## Nash balanced assignment problem

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## Abstract

We consider the Balanced Assignment Problem (BAP) that seeks to find an assignment solution which has the smallest value of max-min distance: the difference between the maximum assignment cost and the minimum one. However, by minimizing only the max-min distance, it may lead to a very inefficient solution in terms of total cost. Hence, we propose a fair way based on Nash equilibrium for finding assignment solutions having a better trade-off between the two objectives. For that, we introduce the concept of Nash Fairness (NF) solutions based on the definition of proportional-fair scheduling. The main result of this paper is to show that finding all NF solutions can be done in polynomial time.

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